



4. Find the missing coordinates for the following points on the unit circle.

a)  $(x, \frac{-4}{3})$  in quadrant 4

b)  $(\frac{2\sqrt{2}}{3}, y)$  in quadrant 4

5. Identify the angle for which the terminal arm intersects the unit circle at  $(\frac{\sqrt{3}}{2}, -\frac{1}{2})$

6. Determine the exact roots for each trig equation over the specified domain.

a.  $\sin\theta = \frac{1}{2}$  ( $0 \leq \theta \leq 2\pi$ )

c.  $\tan\theta = \frac{-\sqrt{3}}{3}$  ( $0 \leq \theta \leq 360^\circ$ )

b.  $\cos\theta = \frac{-\sqrt{3}}{2}$  ( $0 \leq \theta \leq 360^\circ$ )

d.  $\sec\theta = \frac{2}{\sqrt{3}}$  ( $0 \leq \theta \leq 2\pi$ )

7. Solve the following equation using technology

a)  $\sin^2 x + \sin x = 3$

b)  $3\sin x = \frac{1}{2}x^2$

8. Verify that  $x = \frac{\pi}{3}$  is a root of the equation  $\tan^2 x - 3 = 0$

9. Determine approximate values for:

a)  $\tan 42^\circ$

b)  $\csc 193^\circ$

10. If  $\tan \theta = \frac{\sqrt{3}}{3}$  the solutions to  $\theta$  are  $\frac{\pi}{6}$  and  $\frac{7\pi}{6}$  if the domain is  $(0 \leq \theta \leq 2\pi)$ . Write the general solution to each solution.

**Level 3**

11. Write the six trigonometric ratios in terms of  $x$ ,  $y$ , and  $r$  if the point  $(-5, 12)$  is on the terminal arm of the angle. Leave answers in simplest radical form (no decimals).

12. Determine exact roots of each trig equation over the specified domain.

a)  $\sqrt{2} \sin x + 4 = 5 \quad (0 \leq \theta \leq 2\pi)$

c)  $2\cos^2\theta - 7\cos\theta + 3 = 0 \quad (0 \leq \theta \leq 2\pi)$

b)  $\sin^2\theta - \sin\theta = 0 \quad (0 \leq \theta \leq 2\pi)$

d)  $\csc^2\theta - 1 = 0 \quad (0 \leq \theta \leq 180^\circ)$

**Level 4**

13. If  $\theta = \left\{ \frac{\pi}{3}, \frac{5\pi}{3} \right\}$  write a cosine equation with the above solutions over the domain  $(0 \leq \theta \leq 2\pi)$ .

14. Explain why the equation  $\sin^2 x - 5\sin x + 6 = 0$  has no solution.

15. Determine the solution set to each equation for  $(0 \leq \theta \leq 2\pi)$ .

$$\sin x \tan x - \sqrt{3} \sin x + \tan x - \sqrt{3} = 0$$

